













AirfoilPrep.py Documentation Release 0.1.0

S.A. Ning

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Technical Report NREL/TP-5000-58817 September 2013

Contract No. DE-AC36-08GO28308



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Prepared under Task No. WE11.0341

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National Renewable Energy Laboratory 15013 Denver West Parkway Golden, CO 80401 303-275-3000 • www.nrel.gov Technical Report NREL/TP-5000-58817 September 2013

Contract No. DE-AC36-08GO28308

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1 Introduction

AirfoilPrep.py (pronounced Airfoil Preppy) provides functionality to preprocess aerodynamic airfoil data. Essentially, the module is an object oriented version of the AirfoilPrep spreadsheet with additional functionality and is written in the Python language. The intent is to provide the functionality of the AirfoilPrep spreadsheet, but in an easy-to-use format both for stand-alone preprocessing through scripting and for direct implementation within other codes such as blade element momentum methods.

AirfoilPrep.py allows the user to read in two-dimensional (2-D) aerodynamic airfoil data (i.e., from wind tunnel data or numerical simulation), apply three-dimensional (3-D) rotation corrections for wind turbine applications, and extend the data to very large angles of attack. Airfoil data can also be blended together to define intermediate sections between linearly lofted sections. Capabilities unique to the Python version include the ability to read and write to AeroDyn format files directly. The only feature that is contained in the spreadsheet version but is currently missing in AirfoilPrep.py, is handling of pitching moment coefficients.

This document discusses installation, usage, and documentation of the module. Because the theory is simplistic, only a brief overview is provided in the documentation section with corresponding references that contain further detail.

2 Installation

Prerequisites

NumPy

Download either AirfoilPrep.py-0.1.0.tar.gz or AirfoilPrep.py-0.1.0.zip and uncompress/unpack it.

If you are only going to use AirfoilPrep.py from the *command-line* for simple preprocessing, no installation is necessary. The airfoilprep.py file in the src directory can be copied to any location on your computer and used directly. For convenience you may want to add the directory it is contained in to the system path. If you will use AirfoilPrep.py from within Python for more advanced preprocessing or for integration with other codes, AirfoilPrep.py should be installed using:

```
$ python setup.py install
```

To verify that the installation was successful and to run all the unit tests:

```
$ python test/test_airfoilprep.py
```

An "OK" signifies that all the tests passed.

See *module documentation* for more details on usage within Python. To access an HTML version of this documentation with improved formatting and links to the source code, open docs/index.html.

3 Tutorial

AirfoilPrep.py can be accessed either through the *command line* or through *Python*. The command-line interface is the simplest but provides only a limited number of options. The Python interface is useful for more advanced preprocessing and for integration with other codes.

3.1 Command-Line Usage

From the terminal, to see the options, invoke help:

```
$ python airfoilprep.py -h
```

When using the command-line options, all files must be AeroDyn formatted files. The command line provides three main methods for working with files directly: 3-D stall corrections, high angle of attack extrapolation, and a blending operation. In all cases, you first specify the name (and path if necessary) of the file you want to work with:

```
$ python airfoilprep.py airfoil.dat
```

The following optional arguments are available

Table 1. Available flags for using AirfoilPrep.py in command-line mode.

arguments	description
	display help
r/R c/r tsr	3-D rotational corrections near stall
cdmax	high angle of attack extrapolation
other weight	blend with other file using specified weight
outfile	specify a different name for output file
	plot data (for diagnostic purposes) using matplotlib
	output airfoil data using a common set of angles of attack
	r/R c/r tsr cdmax other weight

3.1.1 Stall Corrections

The first method available from the command line is -stall3D, which reads the file, applies rotational corrections, and then writes the data to a separate file. This argument must specify the parameters used for the correction in the format --stall3D r/R c/r tsr, where r/R is the local radius normalized by the rotor radius, c/r is the local chord normalized by the local radius, and tsr is the local tip-speed ratio. For example, if airfoil.dat contained 2-D data with r/R=0.5, c/r=0.15, tsr=5.0, then we would apply rotational corrections to the airfoil using:

```
$ python airfoilprep.py airfoil.dat --stall3D 0.5 0.15 5.0
```

By default the output file will append _3D to the name. In the above example, the output file would be airfoil_- 3D.dat. However, this can be overriden with the --out option. To output to a file at /Users/Me/Airfoils/my_-new_airfoil.dat:

```
$ python airfoilprep.py airfoil.dat --stall3D 0.5 0.15 5.0 \
> --out /Users/Me/Airfoils/my_new_airfoil.dat
```

Optionally, you can also plot the results (matplotlib must be installed) with the --plot flag. For example,

```
$ python airfoilprep.py DU21_A17.dat --stall3D 0.2 0.3 5.0 --plot
```

displays Figure 1 (only one Reynolds number shown) along with producing the output file. AirfoilPrep.py can

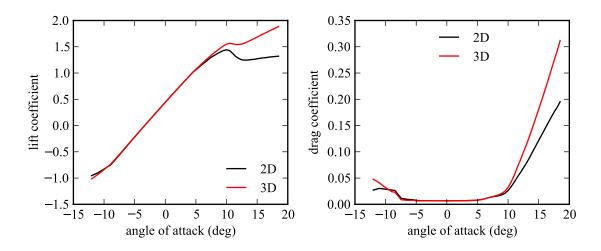


Figure 1. Lift and drag coefficient with 3-D stall corrections applied.

utilize data for which every Reynolds number uses a different set of angles of attack. However, some codes need data on a uniform grid of Reynolds number and angle of attack. To output the data on a common set of angles of attack, use the --common flag.

```
$ python airfoilprep.py airfoil.dat --stall3D 0.5 0.15 5.0 --common
```

3.1.2 Angle of Attack Extrapolation

The second method available from the command line is --extrap, which reads the file, applies high angle of attack extrapolations, and then writes the data to a separate file. This argument must specify the maximum drag coefficient to use in the extrapolation across the full +/- 180-degree range --extrap cdmax. For example, if airfoil_3D.dat contained 3D stall corrected data and cdmax=1.3, then we could extrapolate the airfoil using:

```
$ python airfoilprep.py airfoil_3D.dat --extrap 1.3
```

By default the output file will append _extrap to the name. In the above example, the output file would be airfoil_-3D_extrap.dat. However, this can also be overriden with the --out flag. The --common flag is also useful here if a common set of angles of attack is needed.

The output can be plotted with the -plot flag. The command

```
$ python airfoilprep.py DU21_A17_3D.dat --extrap 1.3 --plot
```

displays Figure 2 (only one Reynolds number shown) along with producing the output file.

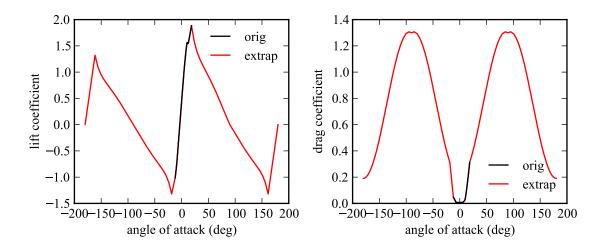


Figure 2. Airfoil data extrapolated to high angles of attack.

3.1.3 Blending

The final capability accessible from the command line is blending of airfoils. This is invoked through <code>--blendfilename</code> weight, where filename is the name (and path if necessary) of a second file to blend with, and weight is the weighting used in the blending. The weight ranges on a scale of 0 to 1 where 0 returns the first airfoil and 1 the second airfoil. For example, the following command blends airfoil1.dat with airfoil2.dat with a weighting of 0.3 (conceptually the new airfoil would equal 0.7*airfoil1.dat + 0.3*airfoil2.dat).

```
$ python airfoilprep.py airfoil1.dat --blend airfoil2.dat 0.3
```

By default, the output file appends the names of the two files with a '+' sign, then appends the weighting using '_blend' and the value for the weight. In this example, the output file would be airfoill+airfoil2_-blend0.3.dat. Just like the previous case, the name of the output file can be overridden by using the --out flag. The --common flag is also useful here if a common set of angles of attack is needed. This data can also be plotted, but only the blended airfoil data will be shown. Direct comparison to the original data is not always possible, because the blend method allows for the specified airfoils to be defined at different Reynolds numbers. Blending first occurs across Reynolds numbers and then across angle of attack.

3.2 Python Usage

The Python interface allows for more flexible usage or integration with other programs. Descriptions of the interfaces for the classes contained in the module are contained in *Module Documentation*.

Airfoils can be created from AeroDyn formatted files,

```
from airfoilprep import Polar, Airfoil
import numpy as np
airfoil = Airfoil.initFromAerodynFile('DU21_A17.dat')
```

or they can be created directly from airfoil data.

```
# first polar
Re = 7e6
```

```
alpha = [-14.50, -12.01, -11.00, -9.98, -8.12, -7.62, -7.11, -6.60, -6.50,
         -6.00, -5.50, -5.00, -4.50, -4.00, -3.50, -3.00, -2.50, -2.00, -1.50,
         -1.00, -0.50, 0.00, 0.50, 1.00, 1.50, 2.00, 2.50, 3.00, 3.50, 4.00,
         4.50, 5.00, 5.50, 6.00, 6.50, 7.00, 7.50, 8.00, 8.50, 9.00, 9.50,
         10.00, 10.50, 11.00, 11.50, 12.00, 12.50, 13.00, 13.50, 14.00, 14.50,
         15.00, 15.50, 16.00, 16.50, 17.00, 17.50, 18.00, 18.50, 19.00, 19.50,
         20.00, 20.50]
c1 = [-1.050, -0.953, -0.900, -0.827, -0.536, -0.467, -0.393, -0.323, -0.311,
      -0.245, -0.178, -0.113, -0.048, 0.016, 0.080, 0.145, 0.208, 0.270, 0.333,
      0.396, 0.458, 0.521, 0.583, 0.645, 0.706, 0.768, 0.828, 0.888, 0.948,
      0.996, 1.046, 1.095, 1.145, 1.192, 1.239, 1.283, 1.324, 1.358, 1.385,
      1.403, 1.401, 1.358, 1.313, 1.287, 1.274, 1.272, 1.273, 1.273, 1.273,
      1.272, 1.273, 1.275, 1.281, 1.284, 1.296, 1.306, 1.308, 1.308, 1.308,
      1.308, 1.307, 1.311, 1.325]
cd = [0.0567, 0.0271, 0.0303, 0.0287, 0.0124, 0.0109, 0.0092, 0.0083, 0.0089,
      0.0082, 0.0074, 0.0069, 0.0065, 0.0063, 0.0061, 0.0058, 0.0057, 0.0057,
      0.0057, 0.0057, 0.0057, 0.0057, 0.0057, 0.0058, 0.0058, 0.0059, 0.0061,
      0.0063, 0.0066, 0.0071, 0.0079, 0.0090, 0.0103, 0.0113, 0.0122, 0.0131,
      0.0139, 0.0147, 0.0158, 0.0181, 0.0211, 0.0255, 0.0301, 0.0347, 0.0401,
      0.0468, 0.0545, 0.0633, 0.0722, 0.0806, 0.0900, 0.0987, 0.1075, 0.1170,
      0.1270, 0.1368, 0.1464, 0.1562, 0.1664, 0.1770, 0.1878, 0.1987, 0.2100]
p1 = Polar(Re, alpha, cl, cd)
# second polar
Re = 9e6
alpha = [-14.24, -13.24, -12.22, -11.22, -10.19, -9.70, -9.18, -8.18, -7.19,
         -6.65, -6.13, -6.00, -5.50, -5.00, -4.50, -4.00, -3.50, -3.00, -2.50,
         -2.00, -1.50, -1.00, -0.50, 0.00, 0.50, 1.00, 1.50, 2.00, 2.50, 3.00,
         3.50, 4.00, 4.50, 5.00, 5.50, 6.00, 6.50, 7.00, 7.50, 8.00, 9.00,
         9.50, 10.00, 10.50, 11.00, 11.50, 12.00, 12.50, 13.00, 13.50, 14.00,
         14.50, 15.00, 15.50, 16.00, 16.50, 17.00, 17.50, 18.00, 18.50, 19.00]
c1 = [-1.229, -1.148, -1.052, -0.965, -0.867, -0.822, -0.769, -0.756, -0.690,
      -0.616, -0.542, -0.525, -0.451, -0.382, -0.314, -0.251, -0.189, -0.120,
      -0.051, 0.017, 0.085, 0.152, 0.219, 0.288, 0.354, 0.421, 0.487, 0.554,
      0.619, 0.685, 0.749, 0.815, 0.879, 0.944, 1.008, 1.072, 1.135, 1.197,
      1.256, 1.305, 1.390, 1.424, 1.458, 1.488, 1.512, 1.533, 1.549, 1.558,
      1.470, 1.398, 1.354, 1.336, 1.333, 1.326, 1.329, 1.326, 1.321, 1.331,
      1.333, 1.340, 1.362]
cd = [0.1461, 0.1263, 0.1051, 0.0886, 0.0740, 0.0684, 0.0605, 0.0270, 0.0180,
      0.0166, 0.0152, 0.0117, 0.0105, 0.0097, 0.0092, 0.0091, 0.0089, 0.0089,
      0.0088, 0.0088, 0.0088, 0.0088, 0.0088, 0.0087, 0.0087, 0.0088, 0.0089,
      0.0090, 0.0091, 0.0092, 0.0093, 0.0095, 0.0096, 0.0097, 0.0099, 0.0101,
      0.0103, 0.0107, 0.0112, 0.0125, 0.0155, 0.0171, 0.0192, 0.0219, 0.0255,
      0.0307, 0.0370, 0.0452, 0.0630, 0.0784, 0.0931, 0.1081, 0.1239, 0.1415,
      0.1592, 0.1743, 0.1903, 0.2044, 0.2186, 0.2324, 0.2455]
p2 = Polar(Re, alpha, cl, cd)
# create airfoil object (can contain as many polars as desired)
af = Airfoil([p1, p2])
```

Blending is easily accomplished just like in the *command-line interface*. There is no requirement that the two airfoils share a common set of angles of attack.

```
airfoil1 = Airfoil.initFromAerodynFile('DU21_A17.dat')
airfoil2 = Airfoil.initFromAerodynFile('DU25_A17.dat')
# blend the two airfoils
airfoil_blend = airfoil1.blend(airfoil2, 0.3)
```

Applying 3-D corrections and high alpha extensions directly in Python, allows for a few additional options as compared to the command-line version. The following example performs the same 3-D correction as in the *command-line version*, followed by an alternative 3-D correction that utilizes some of the optional inputs. See correction3D for more details on the optional parameters.

The airfoil data can be extended to high angles of attack using the extrapolate method. Just like the previous method, a few optional parameters are available through the Python interface. The following example performs the same extrapolation as in the *command-line version*, followed by an alternative extrapolation that utilizes some of the optional inputs.

Some codes need to use the same set of angles of attack data for every Reynolds number defined in the airfoil. The following example performs the same method as in the *command-line version* followed by an alternate approach where the user can specify the set of angles of attack to use.

```
# create new airfoil that uses the same angles of attack at each Reynolds number
af_common1 = af.interpToCommonAlpha()

# default approach uses a union of all defined angles of attack
# alternatively, specify the exact angles to use
```

```
alpha = np.arange(-180, 180)
af_common2 = af.interpToCommonAlpha(alpha)
```

For direct access to the underlying data in a grid format (if not already a grid, it is interpolated to a grid first), use the createDataGrid method as follows:

```
# extract a data grid from airfoil
alpha, Re, cl, cd = af.createDataGrid()
# cl[i, j] is the lift coefficient for alpha[i] and Re[j]
```

Finally, writing AeroDyn formatted files is straightforward.

```
af.writeToAerodynFile('output.dat')
```

4 Module Documentation

Two classes are provided in the module: *Polar* and *Airfoil*. Generally, the Polar class is not needed for direct usage except for its constructor. All objects in this module are **immutable**. In other words, calling Airfoil.correct3D() creates a new modified airfoil object rather than editing the existing object.

This PDF version of the documentation only provides an summary of the classes and methods. Further details are found in the HTML version of this documentation, complete with hyperlinks to the source code.

4.1 Polar Class

A Polar object is meant to represent the variation in lift, drag, and pitching moment coefficient with angle of attack at a fixed Reynolds number. Generally, the methods of this class do not need to be used directly (other than the constructor), but rather are used by the Airfoil class.

```
Class Summary:
class airfoilprep.Polar (Re, alpha, cl, cd)
     Constructor
           Parameters
               Re: float
                   Reynolds number
               alpha: ndarray (deg)
                   angle of attack
               cl: ndarray
                   lift coefficient
               cd : ndarray
                   drag coefficient
     blend(other, weight)
           Blend this polar with another one with the specified weighting
               Parameters
                   other: Polar
                     another Polar object to blend with
                   weight: float
                     blending parameter between 0 and 1. 0 returns self, whereas 1 returns other.
               Returns
                   polar: Polar
                     a blended Polar
     correction3D (r_over_R, chord_over_r, tsr, alpha_max_corr=30, alpha_linear_min=-5, alpha_-
                        linear\ max=5)
           Applies 3-D corrections for rotating sections from the 2-D data.
```

Parameters

 r_over_R : float

local radial position / rotor radius

chord_over_r: float

local chord length / local radial location

tsr: float

tip-speed ratio

alpha_max_corr: float, optional (deg)

maximum angle of attack to apply full correction

alpha_linear_min: float, optional (deg)

angle of attack where linear portion of lift curve slope begins

alpha_linear_max : float, optional (deg)

angle of attack where linear portion of lift curve slope ends

Returns

polar : Polar

A new Polar object corrected for 3-D effects

Notes

The Du-Selig method (Du and Selig, 1998) is used to correct lift, and the Eggers method (Eggers Jr et al., 2003) is used to correct drag.

```
extrapolate (cdmax, AR=None, cdmin=0.001, nalpha=15)
```

Extrapolates force coefficients up to +/- 180 degrees using Viterna's method (Viterna and Janetzke, 1982).

Parameters

cdmax: float

maximum drag coefficient

AR: float, optional

aspect ratio = (rotor radius / chord_75% radius) if provided, cdmax is computed from AR

cdmin: float, optional:

minimum drag coefficient. used to prevent negative values that can sometimes occur with this extrapolation method

nalpha: int, optional:

number of points to add in each segment of Viterna method

Returns

polar: Polar

a new Polar object

Notes

If the current polar already supplies data beyond 90 degrees then this method cannot be used in its current form and will just return itself.

If AR is provided, then the maximum drag coefficient is estimated as

```
wnsteadyparam (alpha_linear_min=-5, alpha_linear_max=5)
compute unsteady aero parameters used in AeroDyn input file

Parameters
    alpha_linear_min: float, optional (deg)
    angle of attack where linear portion of lift curve slope begins

alpha_linear_max: float, optional (deg)
    angle of attack where linear portion of lift curve slope ends

Returns
    aerodynParam: tuple of floats
    (control setting, stall angle, alpha for 0 cn, cn slope, cn at stall+, cn at stall-, alpha for
```

4.2 Airfoil Class

An Airfoil object encapsulates the aerodynamic forces/moments of an airfoil as a function of angle of attack and Reynolds number. For wind turbine analysis, this class provides capabilities to apply 3-D rotational corrections to 2-D data using the Du-Selig method (Du and Selig, 1998) for lift, and the Eggers method (Eggers Jr et al., 2003) for drag. Airfoil data can also be extrapolated to +/-180 degrees, using Viterna's method (Viterna and Janetzke, 1982). This class also adds methods to read and write AeroDyn airfoil files directly.

Class Summary:

```
class airfoilprep.Airfoil (polars)
    Constructor

Parameters
    polars: list(Polar)
    list of Polar objects

blend (other, weight)
    Blend this Airfoil with another one with the specified weighting.

Parameters
    other: Airfoil
    other airfoil to blend with

weight: float

blending parameter between 0 and 1. 0 returns self, whereas 1 returns other.
```

min CD, min(CD))

```
Returns
```

obj : Airfoil

a blended Airfoil object

Notes

First finds the unique Reynolds numbers. Evaluates both sets of polars at each of the Reynolds numbers, then blends at each Reynolds number.

```
correction3D (r_over_R, chord_over_r, tsr, alpha_max_corr=30, alpha_linear_min=-5, alpha_-
     linear_max=5)
apply 3-D rotational corrections to each polar in airfoil
          Parameters
              r over R: float
                radial position / rotor radius
              chord\_over\_r: float
                local chord / local radius
              tsr: float
                tip-speed ratio
              alpha_max_corr : float, optional (deg)
                maximum angle of attack to apply full correction
              alpha_linear_min : float, optional (deg)
                angle of attack where linear portion of lift curve slope begins
              alpha_linear_max : float, optional (deg)
                angle of attack where linear portion of lift curve slope ends
          Returns
              airfoil: Airfoil
                airfoil with 3-D corrections
     See Also:
     Polar.correction3D
          apply 3-D corrections for a Polar
createDataGrid()
     interpolate airfoil data onto uniform alpha-Re grid.
          Returns
              alpha: ndarray (deg)
                a common set of angles of attack (union of all polars)
              Re: ndarray
                all Reynolds numbers defined in the polars
```

cl: ndarray

lift coefficient 2-D array with shape (alpha.size, Re.size) cl[i, j] is the lift coefficient at alpha[i] and Re[j]

cd: ndarray

drag coefficient 2-D array with shape (alpha.size, Re.size) cd[i, j] is the drag coefficient at alpha[i] and Re[j]

extrapolate(cdmax, AR=None, cdmin=0.001)

apply high alpha extensions to each polar in airfoil

Parameters

cdmax: float

maximum drag coefficient

AR: float, optional

blade aspect ratio (rotor radius / chord at 75% radius). if included it is used to estimate cdmax

cdmin: minimum drag coefficient:

Returns

airfoil: Airfoil

airfoil with +/-180 degree extensions

See Also:

Polar.extrapolate

extrapolate a Polar to high angles of attack

getPolar(Re)

Gets a Polar object for this airfoil at the specified Reynolds number.

Parameters

Re: float

Reynolds number

Returns

obj: Polar

a Polar object

Notes

Interpolates as necessary. If Reynolds number is larger than or smaller than the stored Polars, it returns the Polar with the closest Reynolds number.

${\bf classmethod\ init} {\bf From} {\bf Aerodyn} {\bf File}\ (aerodyn File)$

Construct Airfoil object from AeroDyn file

Parameters

aerodynFile: str

path/name of a properly formatted Aerodyn file

Returns

obj : Airfoil

interpToCommonAlpha(alpha=None)

Interpolates all polars to a common set of angles of attack

Parameters

alpha: ndarray, optional

common set of angles of attack to use. If None a union of all angles of attack in the polars is used.

writeToAerodynFile (filename)

Write the airfoil section data to a file using AeroDyn input file style.

Parameters

filename: str

name (+ relative path) of where to write file

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